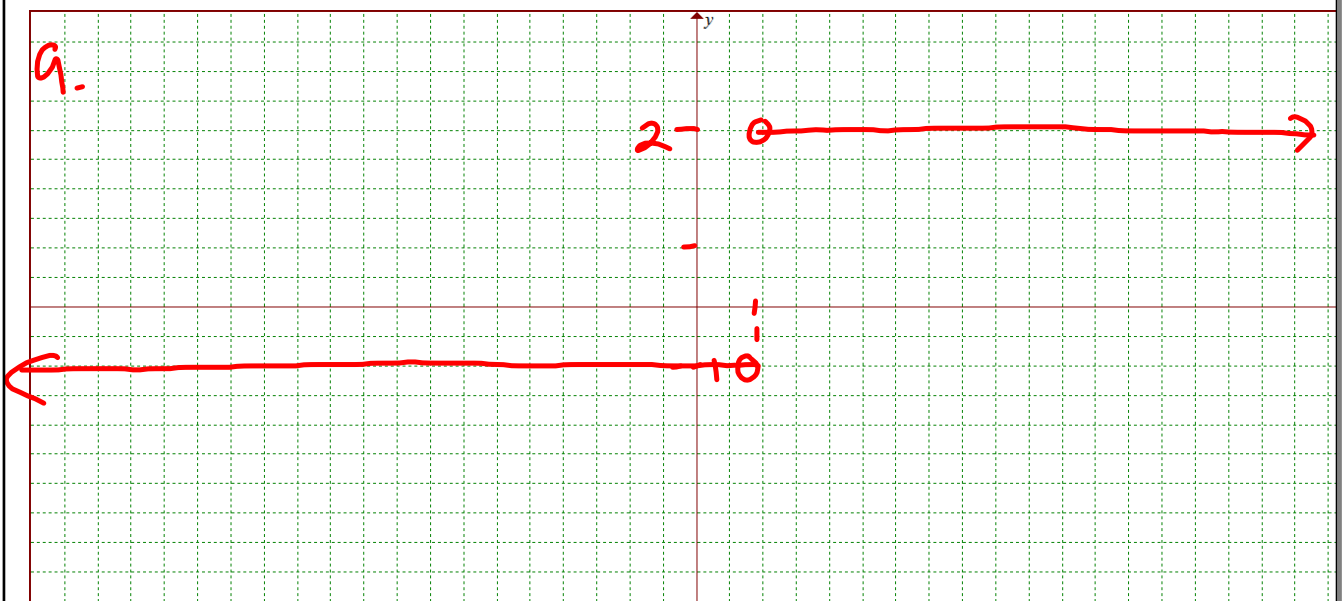
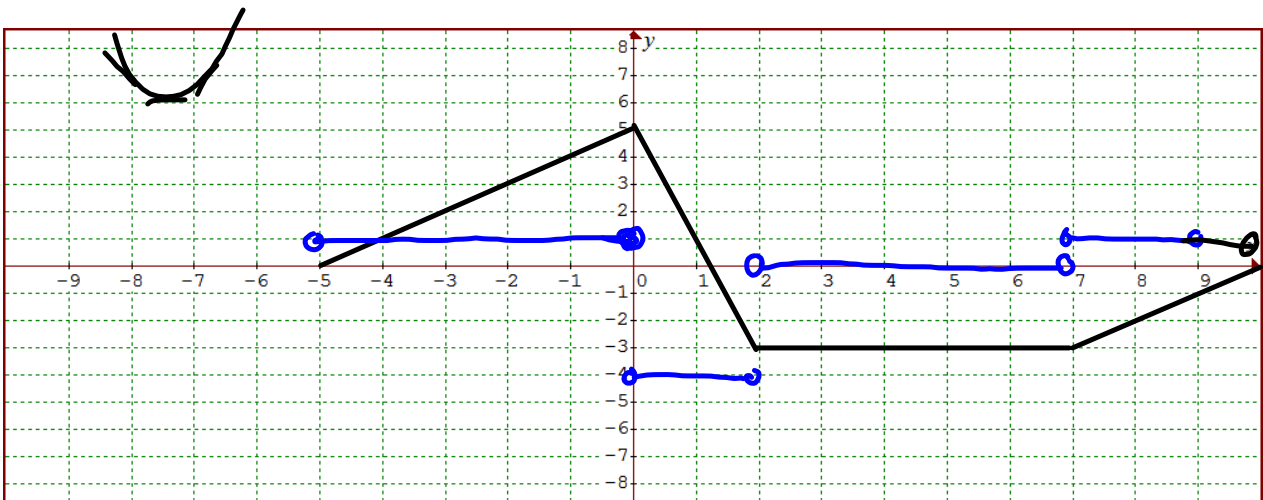




A piecewise function is shown below. Graph the derivative of this function.



$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\lim_{h \rightarrow 0} \frac{3(x+h)^2 + 2(x+h) + 1 - (3x^2 + 2x + 1)}{h}$$

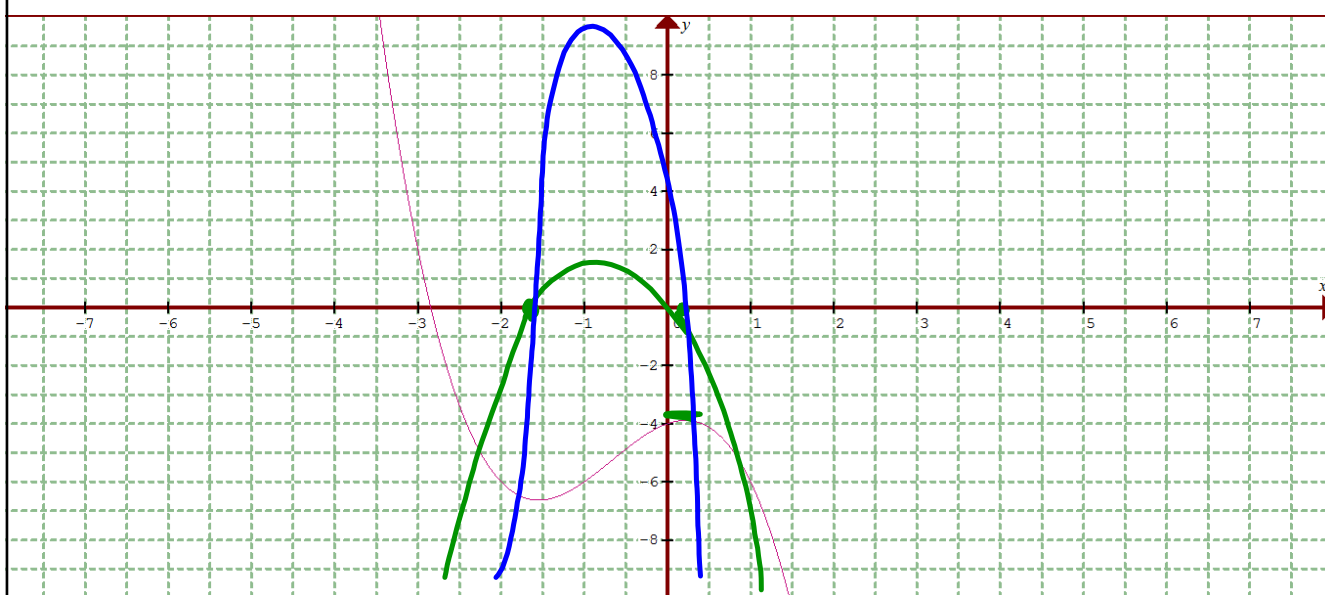
$$\lim_{h \rightarrow 0} \frac{3(\cancel{x^2} + 2xh + \cancel{h^2}) + \cancel{2x} + 2h + \cancel{1} - \cancel{3x^2} - \cancel{2x} - \cancel{1}}{h}$$

$$\lim_{h \rightarrow 0} \frac{6xh + 3h^2 + 2h}{h}$$

$$\lim_{h \rightarrow 0} \frac{6x + 3h + 2}{1}$$

$$f'(x) = 6x + 2$$

Sketch a possible graph of  $f'(x)$  using the graph of  $f(x)$  below:



Calculus 120

Unit 1: Rate of Change and Derivatives

February 14, 2019: Day #9

1. Test on ~~Wednesday~~ *Thursday*
2. Assignment Due on ~~Friday?~~ *Tuesday*
3. Quiz

### **Curriculum Outcomes**

**C1.** Explore the concepts of average and instantaneous rate of change.

**C2.** Determine the derivative of a function by applying the definition of derivative.

## Differentiability of Functions

A function is said to be **differentiable** at "a" if  $f'(a)$  exists.

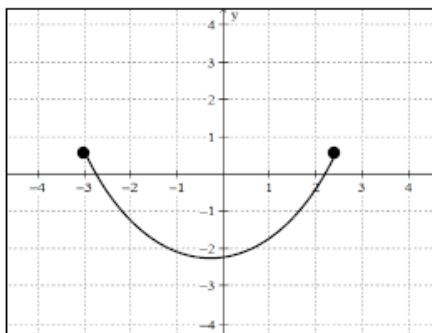
A function is said to be **differentiable on an interval** if it is differentiable at every number in the interval.

A **right-hand derivative** is a derivative defined by a right-hand limit.

A **left-hand derivative** is a derivative defined by a left-hand limit.

**There are five situations in which relations are not differentiable:**

1. Functions with restricted domains are not differentiable at their endpoints.



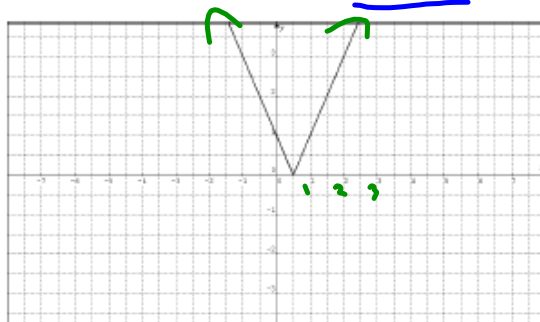
This function is differentiable on what interval?

$(-3, 2.4)$

At what point(s) is it not differentiable?

$x = -3$  &  $x = 2.4$   
 $(-3, 0.7)$  &  $(2.4, 0.7)$

2. Functions are not differentiable at corners.



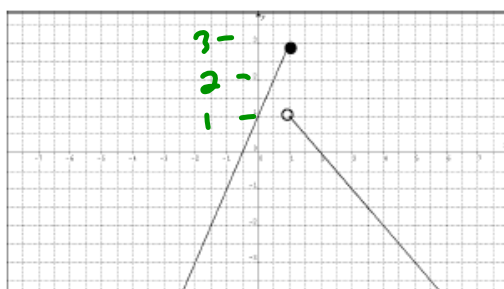
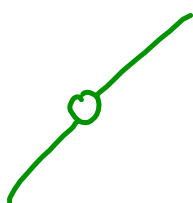
At what point is this function not differentiable?  $x=0,5$   $(0,5,0)$

Where is the function differentiable?

$$(-\infty, 0,5) \cup (0,5, \infty)$$



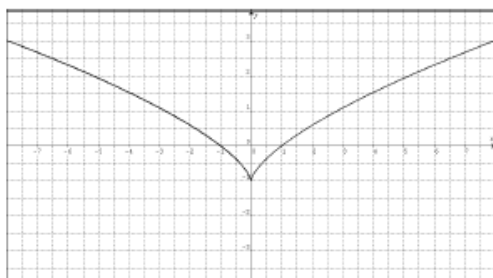
3. Functions are not differentiable at points of discontinuity.



Where is this function not differentiable?

@  $x=1$   
 $(1,1)$  or  $(1,3)$

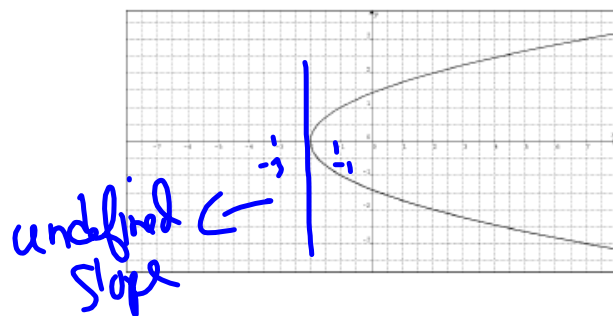
4. Functions are not differentiable at cusps. *curvy / corner*



Where is this function not differentiable?

$$x = 0$$

5. Functions are not differentiable at points where vertical tangents occur.



At what point is this function not differentiable?

$x = -2 \rightarrow (-2, 0)$

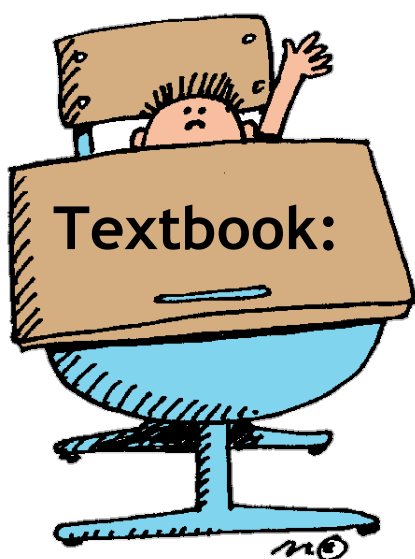
Ex: Determine the values of  $x$  for which the following functions are not differentiable? Provide reasoning.

$$y = \frac{1}{x-2}$$


$$y = |x+4| - 1$$

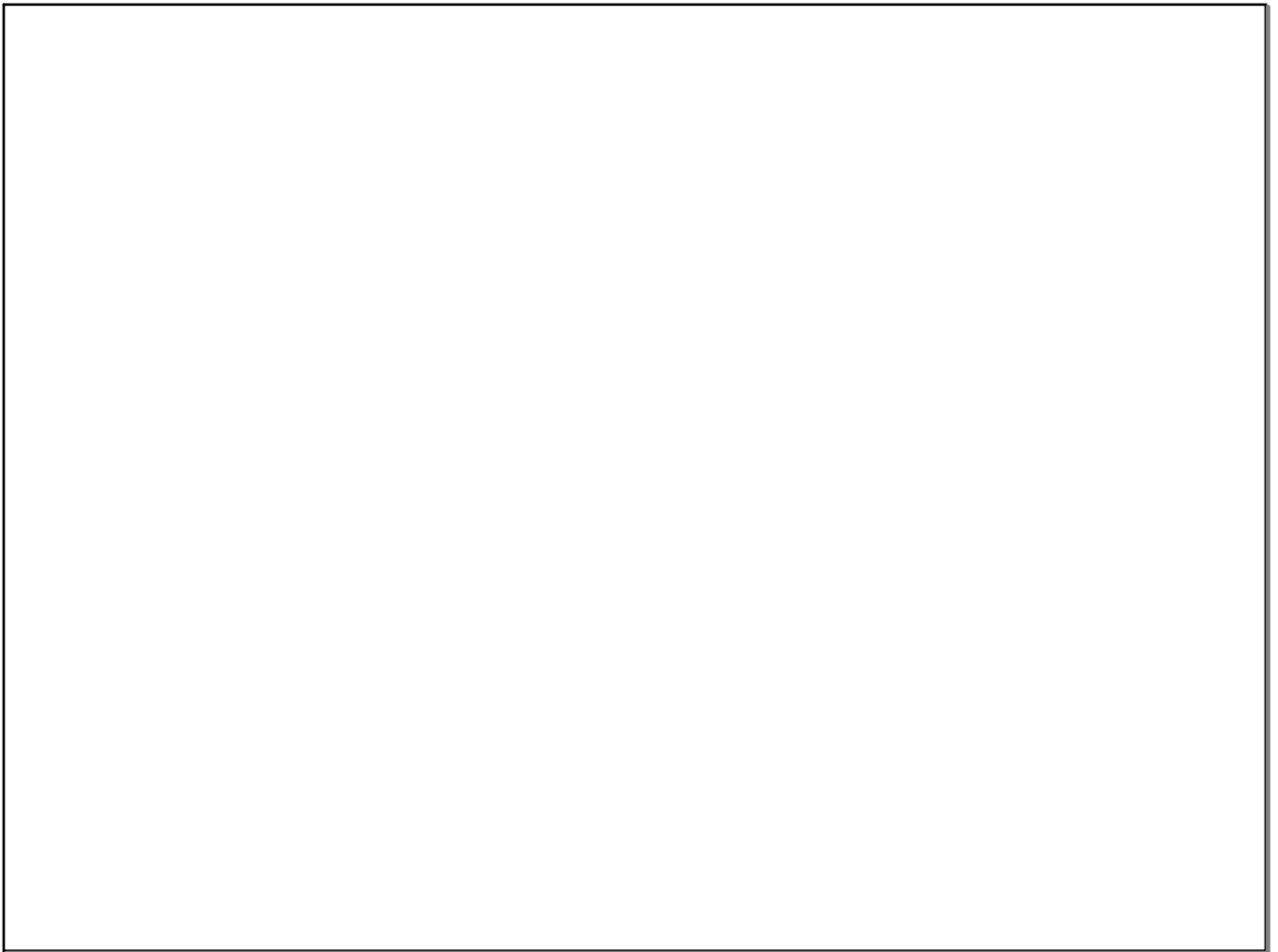
$$y = (x-1)^{\frac{2}{3}}$$

$$y = 2\sqrt{x+5} - 2$$



Practice

 Page 114-115 Green Book  
#5, 7, 9, 11-16



## Attachments

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2.1\_74\_AP.html



2.1\_74\_AP.swf



2.1\_74\_AP.html